



# THE GURUKUL INSTITUTE

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PHYSICS

## HEAT & THERMODYNAMICS

### HEAT/THERMAL EXPANSION

1. What is the unit of heat?

2. (i) Take a metallic cylindrical vessel of steel of internal volume  $V_0$  and a solid cylinder of steel of similar shape and volume  $V_0$ . The temperature of both is raised up to  $\Delta T$ . Can we put the solid inside the vessel?

(ii) A silver ring is tightly fitted on a silver rod. Can we remove the ring from the rod by raising or lowering the temperature?

3. A steel glass is half filled with a liquid. The coefficients of volume expansion of steel and liquid are same. When temperature is increased, the volume of empty glass increases or decreases. If temperature is decreased, what will happen to the empty glass volume.

4. A sphere of silver is floating in a mercury bath. If temperature is increased, will the sphere sink deeper or rise? It is given

$$\gamma_{\text{Silver}} > \gamma_{\text{Mercury}}$$

5. A sphere of diameter 7 cm and mass 266.5 gm floats in a bath of liquid. As the temperature is raised, the sphere just sinks at a temperature of  $35^\circ\text{C}$ . If the density of the liquid at  $0^\circ\text{C}$  is  $1.527 \text{ gm/cm}^3$ , find the coefficient of cubical expansion of the liquid. ( $\gamma$  of sphere is negligible)

6. A cubical block is floating inside a bath. The temperature of system is increased by small temperature  $\Delta T$ . It was found that the depth of submerged portion of cube does not change. Find the relation between coefficient of linear expansion ( $\alpha$ ) of the cube and volume expansion of liquid ( $\gamma$ ).

7. A light steel wire of length  $L$  and area of cross-section  $A$  is hanging vertically downward from a ceiling. It cools to the room temperature ( $30^\circ\text{C}$ ) from the initial temperature  $100^\circ\text{C}$ . Calculate the weight which should be attached at its lower end such that its length remains same. Young's modulus of steel is  $Y$  and coefficient of linear expansion is  $\alpha$ .

### CALORIMETRY: Principle of Calorimetry

8. Find the molar heat capacity of the process  $P = a/T$  for a monatomic gas, 'a' being positive constant.

9. A gaseous mixture enclosed in a vessel consists of one gm mole of a gas A with  $\gamma = (5/3)$  and some amount of gas B with  $\gamma = 7/5$  at a temperature  $T$ . The gases A and B do not react with each other and are assumed to be ideal. Find the number of gm moles of the gas B if  $\gamma$  for the gaseous mixture is  $(19/13)$ .

10. An air bubble starts rising from the bottom of a lake. Its diameter is 3.6 mm at the bottom and 4 mm at the surface. The depth of the lake is 250 cm and the temperature at the surface is  $40^\circ\text{C}$ . What is the temperature at the bottom of the lake? Given atmospheric pressure = 76 cm of Hg and  $g = 980 \text{ cm/sec}^2$ . (Specific gravity of mercury = 13.6)

11. Can an ideal gas be liquefied?

12. Two different gases have exactly the same temperature. Does this mean that their molecules have the same rms speed?

13. Given: Avogadro's number  $N = 6.02 \times 10^{23}$  and Boltzmann's constant  $k = 1.38 \times 10^{-23} \text{ J/K}$ .

(i) Calculate the average kinetic energy of translation of the molecules of an ideal gas at  $0^\circ\text{C}$  and at  $100^\circ\text{C}$ .

(ii) Also calculate the corresponding energies per mole of the gas.

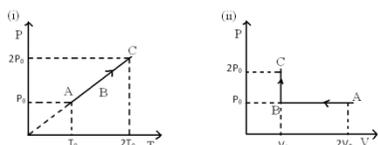
### DEGREES OF FREEDOM

14. How many degrees of freedom does the gas molecule have if under standard conditions the gas density is  $1.3 \text{ kg/m}^3$  and the velocity of sound in it is  $v = 330 \text{ m/s}$ .

15. One mole of an ideal monatomic gas is taken at a temperature of 300 K. Its volume is doubled keeping its pressure constant. Find the change in internal energy.

16. Two moles of a diatomic ideal gas is taken through the process  $PT = \text{const}$ . Its temperature is increased from  $T_0 \text{ K}$  to  $2T_0 \text{ K}$ . Find the work done by the system?

17. Three moles of a diatomic gas is taken through the process A-B-C as shown in the figure. Find work done by the system in the process A-B-C.



18. At 1 atmospheric pressure, 1.000 gm of water having a volume of  $1.000 \text{ cm}^3$  becomes  $1.091 \text{ cm}^3$  of ice on freezing. The heat of fusion of water at 1 atmosphere is  $80.0 \text{ cal/gm}$ . What is the change in internal energy during the process?

19. An ideal monatomic gas at temperature  $27^{\circ}\text{C}$  and pressure  $10^6 \text{ N/m}^2$  occupies 10 litre volume. 10,000 cal of heat is added to the system without changing the volume. Calculate the final temperature of the gas. Given:  $R=8.31 \text{ J/(mol}\cdot\text{K)}$  and  $J= 4.18 \text{ J/ cal}$ .

### HEAT TRANSFER

20. (i) Pieces of copper and glass are heated to the same temperature. Why do the pieces of copper feel hotter on touching? At what common temperature do the pieces of copper and glass feel equally hot when touched?

(ii) Thermal conductivity of air is less than of felt, but felt is a better heat insulator in comparison to air, why?

21. Two plates each of area  $A$ , thicknesses  $L_1$  and  $L_2$  and thermal conductivities  $K_1$  and  $K_2$  are joined to form a single plate of thickness  $(L_1+L_2)$ . If the temperatures of the free surfaces are  $T_1$  and  $T_2$ , calculate

- rate of flow of heat;
- temperature of interface; and
- equivalent thermal conductivity.

22. A cylinder of radius  $R$  made of a material of thermal conductivity  $K_1$  is surrounded by a cylindrical shell of inner radius  $R$  and outer radius  $2R$  made of a material of thermal conductivity  $K_2$ . The two ends of the combined system are maintained at two different temperatures.

There is no loss of heat across the cylindrical surface and the system is in steady state. What is the effective thermal conductivity of the system?

23. Find the rate of heat flow and temperature as a function of radius  $r$  in case of a cylindrical shell whose inner surface temperature and outer surface temperature are  $\theta_1$  and  $\theta_2$ . The inner and the outer radii of the cylindrical shell are  $r_1$  and  $r_2$ .

24. On a winter night you feel warmer when clouds cover the sky than when the sky is clear. Why?

25. A metallic ball has a black spot. The ball is heated to  $1000^{\circ}\text{C}$  and is then taken into a dark room. It is found that black spot looks brighter than rest of the ball. How can you understand this?

26. Two bodies A and B have thermal emissivities of 0.01 and 0.81. The outer surface areas of the two bodies are same. The two bodies emit total radiant power at the same rate. The wavelength  $\lambda_B$  corresponding to maximum spectral radiancy in the radiation from B is shifted from the wavelength corresponding to maximum spectral radiancy in the radiation from A by  $1.00\mu\text{m}$ . If the temperature of A is  $5802 \text{ K}$ , calculate:

- the temperature of B and
- wavelength  $\lambda_B$ .

### PROBLEMS

1. A bar of length  $L_0$  is heated from temperature  $t_1$  to  $t_2$ . Find the final length of bar if its coefficient of linear expansion of linear expansion varies according to equation  $\alpha = aL$ , where  $a$  is constant and  $L$  is the length of bar.

2. Two glass bulbs of volumes  $500 \text{ cm}^3$  and  $100 \text{ cm}^3$  are connected by a narrow tube whose volume is negligible. When the apparatus is sealed off, the pressure of the air inside is  $70 \text{ cm}$  of mercury and its temperature is  $20^{\circ}\text{C}$  and the other is heated to  $100^{\circ}\text{C}$ .

3. One mole of an ideal gas whose pressure changes with volume as  $P = \alpha V$ , where  $\alpha$  is a constant, is expanded so that its volume increases  $n$  times. Find the work done and change in internal energy. [Adiabatic exponent =  $\gamma$ ]

4. An ideal gas is taken through a cyclic thermodynamic process through four steps. The amounts of heat involved in these steps are  $Q_1=5960 \text{ J}$ ;  $Q_2=-5585 \text{ J}$ ;  $Q_3=-2980 \text{ J}$ ; and  $Q_4=3645 \text{ J}$ . The corresponding work involved are  $W_1=2200 \text{ J}$ ;  $W_2=-825 \text{ J}$ ;  $W_3=-1100 \text{ J}$  and  $W_4$ , respectively.

(a) Find the value of  $W_4$ .

(b) What is the efficiency of the cycle?

5. At  $27^{\circ}\text{C}$ , two moles of an ideal monoatomic gas occupy a volume  $V$ . The gas expands adiabatically to a volume  $2V$ . Calculate:

(a) final temperature of the gas;

(b) change in its internal energy; and

(c) the work done by the gas during the process. [ $R= 8.31 \text{ J/ mol K}$ ]

6. One mole of a monoatomic ideal gas is taken through the cycle shown in figure.

A  $\rightarrow$  B Adiabatic expansion;

B  $\rightarrow$  C Cooling at constant volume;

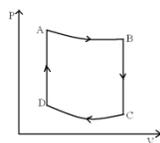
C  $\rightarrow$  D Adiabatic compression;

D  $\rightarrow$  A Heating at constant volume

The pressure and temperature at A, B, etc. are denoted by  $P_A, T_A; P_B, T_B$ ; etc., respectively.

Given  $T_A= 1000\text{K}$ ,  $P_B=(2/3)P_A$  and  $P_C= (1/3)P_A$ . Calculate (a) The work done by the gas in the process A $\rightarrow$ B; (b) the heat lost by the gas in the process B $\rightarrow$ C; and (c) temperature  $T_D$ .

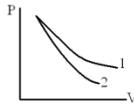
[ Given;  $(2/3)^{2/5} = 0.85$  and  $R= 8.31 \text{ J/ mol K}$ .]



7. A fixed mass of a gas is taken through a process  $A \rightarrow B \rightarrow C \rightarrow A$ . Here  $A \rightarrow B$  is isobaric,  $B \rightarrow C$  is adiabatic and  $C \rightarrow A$  is isothermal.  
Find: (a) pressure and a volume at C;  
(b) work done in the process (take  $\gamma=1.5$ )
8. Find temperature as a function of radius  $r$  in case of hollow sphere having inner and outer radii  $r_1$  and  $r_2$ , maintained at temperature  $\theta_1$  and  $\theta_2$ , respectively.
9. One end of a rod of length 20 cm is inserted in a furnace at 800 K. The sides of the rod are covered with an insulating material and the other end emits radiation like a blackbody. The temperature of this end is 750 K in the steady state. The temperature of the surrounding air is 300 K. Assuming radiation to be the only important mode of energy transfer between the surrounding and the open end of the rod, find the thermal conductivity of the rod. [Stefan's constant  $\sigma = 6.0 \times 10^{-8} \text{ W/m}^2\text{-K}^4$ ]
10. A cylindrical block of length 0.4 m and area of cross-section  $0.04 \text{ m}^2$  is placed coaxially on a thin metal disc of mass 0.4 kg and same cross-section. The upper face of the cylinder is maintained at a constant temperature of 400 K and the initial temperature of the disc is 300 K. If the thermal conductivity of the material of the cylinder is  $10 \text{ W/mK}$  and the specific heat of the material of the disc is  $600 \text{ J/kg K}$ , how long will it take for the temperature of the disc to increase to 350 K? Assume for purpose of calculation the thermal conductivity of the disc to be very high and the system to be thermally insulated except for the upper and lower face of the cylinder.

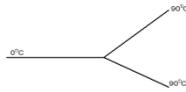
### OBJECTIVE

1. Two rods of length  $L_1$  and  $L_2$  are made of materials whose coefficients of linear expansion are  $\alpha_1$  and  $\alpha_2$ . If the difference between the two lengths is independent of temperature, then  
a)  $L_1/L_2 = \alpha_1/\alpha_2$       b)  $L_1/L_2 = \alpha_2/\alpha_1$       c)  $L_2^2\alpha_1 = L_1^2\alpha_2$   
d)  $\alpha_1^2/L_1 = \alpha_2^2/L_2$
2. Water of volume 2 litre in a container is heated with a coil of 1kW at  $27^\circ\text{C}$ . The lid of the container is open and energy is dissipated at the rate of 160J/s. In how much time temperature will rise from  $27^\circ\text{C}$  to  $77^\circ\text{C}$ ? (Given  $C_{\text{water}} = 4.2\text{kJ/kg}$ )  
a) 8min 20s      b) 6min 2s      c) 2s      d) 14 min
3. A monoatomic gas ( $\gamma = 5/3$ ) is suddenly compressed to  $(1/8)^{\text{th}}$  its volume adiabatically the pressure of the gas will change to  
a) 24/5      b) 8      c) 40/3      d) 32
4. At room temperature the rms speed of the molecules of a certain diatomic gas is found to be 1930 m/s. The gas is  
a)  $\text{H}_2$       b)  $\text{F}_2$       c)  $\text{O}_2$       d)  $\text{Cl}_2$
5. The average translation energy and the rms speed of molecules in a sample of oxygen at 300K are  $6.21 \times 10^{-21} \text{ J}$  and 484 m/s respectively. The corresponding values at 600 K are nearly (assuming ideal gas behavior).  
a)  $12.42 \times 10^{-21} \text{ J}$ , 968 m/s.      c)  $6.21 \times 10^{-21} \text{ J}$ , 968 m/s  
b)  $8.78 \times 10^{-21} \text{ J}$ , 684 m/s      d)  $12.42 \times 10^{-21} \text{ J}$ , 684 m/s
6. Two identical containers A and B with frictionless pistons contains the same ideal gas at the same temperature and the same volume  $V$ . The mass of gas contained in A is  $m_A$  and that in B is  $m_B$ . The gas in each cylinder is now allowed to expand isothermally to the same final volume  $2V$ . The change in the pressure in A and B are found to be  $\Delta P$  and  $1.5\Delta P$ , respectively, then  
a)  $4m_A = 9m_B$       b)  $2m_A = 3m_B$       c)  $3m_A = 2m_B$       d)  $9m_A = 4m_B$
7. Two insulating cylinders A and B fitted with pistons contain equal amounts of an ideal diatomic gas at temperature 300K. The piston A is free to move, while that of B is held fixed. The same amount of heat is given to the gas in each cylinder. If the rise in temperature of the gas in A is 30K, then the rise in temperature of the gas in B is  
a) 30K      b) 18K      c) 50K      d) 42K
8. The volume of a gas at constant pressure of  $10^3 \text{ N/m}^2$  expands by  $0.25 \text{ m}^3$ . The work done by the gas is equal to  
a) 2.3 erg      b) 250J      c) 250 W      d) 250N
9. P-V plots for two gases during adiabatic processes are shown in the figure. Plots 1 and 2 should correspond, respectively to  
a) He and  $\text{O}_2$       b)  $\text{O}_2$  and He      c) He and Ar      d)  $\text{O}_2$  and  $\text{N}_2$



10. A rigid container with thermally insulated walls contains a coil of resistance 100Ω carrying current 1 A. Change in internal energy after 5 minute will be  
a) 0 kJ      b) 10kJ      c) 20kJ      d) 30kJ
11. An ideal gas expands isothermally from a volume  $V_1$  to  $V_2$  and is then compressed to original volume  $V_1$  adiabatically. Initial pressure was  $P_1$  and final pressure is  $P_3$ . The total work done is  $W$ . Then  
a)  $P_3 > P_1$ ,  $W > 0$       b)  $P_3 < P_1$ ,  $W < 0$       c)  $P_3 > P_1$ ,  $W < 0$   
d)  $P_3 = P_1$ ,  $W = 0$

12. Three rods made of the same material and having the same cross-section have been joined as shown in the figure. Each rod is of the same length. The left and right ends are kept at  $0^{\circ}\text{C}$  and  $90^{\circ}\text{C}$  respectively. The temperature of the junction of the three rods will be
- a)  $45^{\circ}\text{C}$       b)  $60^{\circ}\text{C}$       c)  $30^{\circ}\text{C}$       d)  $20^{\circ}\text{C}$



13. Two identical conducting rods are first connected independently to two vessel, one containing water at  $100^{\circ}\text{C}$  and the other containing ice at  $0^{\circ}\text{C}$ . In the second case, the rods are joined end to end and connected to the same vessels. Let  $q_1$  and  $q_2$  be the rate of melting of ice in two cases, respectively. The ratio  $q_1/q_2$  is
- a)  $1/2$       b)  $2/1$       c)  $4/1$       d)  $1/4$
14. Three discs A, B and C having radii 2m, 4m and 6m, respectively, are coated with carbon black on their outer surfaces. The wavelengths corresponding to maximum intensity are 300 nm, 400 nm and 500 nm, respectively. The powers radiated by them are  $Q_A$ ,  $Q_B$  and  $Q_C$  respectively. Then
- a)  $Q_A$  is maximum      b)  $Q_B$  is maximum      c)  $Q_C$  is maximum
- d)  $Q_A=Q_B=Q_C$
15. In a room where the temperature is  $30^{\circ}\text{C}$ , a body cools from  $61^{\circ}\text{C}$  to  $59^{\circ}\text{C}$  in 4 minutes. The time taken by the body to cool from  $51^{\circ}\text{C}$  to  $49^{\circ}\text{C}$  will be:
- a) 4 minutes      b) 6 minutes      c) 5 minutes      d) 8 minutes

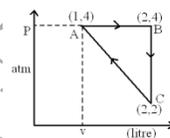
## ASSIGNMENTS

### SECTION- I

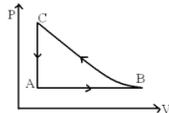
#### PART-A

#### LEVEL-I

- The volume of a thin brass vessel and the volume of a solid cube are both equal to 1 it. What will be change in volumes of vessel and the cube on being heated to  $25^{\circ}\text{C}$ ? Given  $\alpha$  for brass =  $1.9 \times 10^{-5}/^{\circ}\text{C}$ .
- One mole of a monoatomic gas is mixed with 3 moles of a diatomic gas. What is the molecular specific heat of the mixture at constant pressure?
- 30 gm of ice at  $-14^{\circ}\text{C}$  is added to 200 gm of water at  $25^{\circ}\text{C}$ . Find the equilibrium temperature. [Take specific heat of ice =  $0.5 \text{ cal/g} \cdot ^{\circ}\text{C}$ , and latent heat of ice =  $80 \text{ cal/g}$ ]
- At what temperature the rms velocity is equal to escape velocity from the surface of earth for hydrogen and for oxygen? Given radius of earth =  $6.4 \times 10^6 \text{ m}$ ,  $g = 9.8 \text{ m/s}^2$ ;  $k = 1.38 \times 10^{-23} \text{ J/k}$
- A cylinder containing one mole of a monoatomic gas at  $127^{\circ}\text{C}$  expand isothermally until its volume is doubled, and then compressed adiabatically until its temperature rise from  $127^{\circ}\text{C}$  to  $227^{\circ}\text{C}$ . Calculate total work done and heat absorbed.
- A P-V diagram for a cyclic process is a triangle ABC. Calculate work done during the process AB, BC and CA. Also calculate the work done in the complete cycle.



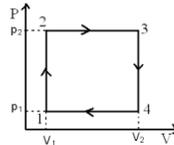
7. Consider the cyclic process ABCA on a sample of 2 mole of an ideal gas as shown in the figure. The temperature of the gas at A and B are 300 K and 500K, respectively. A total of 1200J heat is withdrawn from the sample in the process. Find the work done by the gas in part BC. [ Take  $R = 8.3 \text{ J/ mol} \cdot \text{K}$ ]



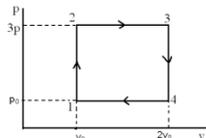
- A sphere, a cube and a thin circular plate all made of the same material and having the same mass are initially heated to  $200^{\circ}\text{C}$ . Which of these objects will cool faster and which one slowest when left in air at room temperature?
- A body which has a surface area of  $5 \text{ cm}^2$  and temperature of  $727^{\circ}\text{C}$  radiates 300 J of energy each minute. What is its emissivity? ( $\sigma = 5.67 \times 10^{-8} \text{ W/m}^2\text{K}^4$ )
- A body cools in 7 minutes from  $60^{\circ}\text{C}$  to  $40^{\circ}\text{C}$ . What will be its temperature after the next 7 minutes? The temperature of surrounding is  $10^{\circ}\text{C}$ .

## LEVEL – II

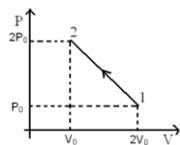
1. A brass disc at  $20^{\circ}\text{C}$  has a diameter of 30 cm and a hole (10 cm in diameter) is cut inside the disc. Calculate the diameter of hole when temperature of the disc is raised to  $50^{\circ}\text{C}$ . [The coefficient of linear expansion of brass =  $0.000018/^{\circ}\text{C}$ .]
2. A steel wire of cross sectional area  $0.5\text{ mm}^2$  is held between two fixed supports. The tension in the wire is negligible and it is just taut at a temperature of  $20^{\circ}\text{C}$ . Determine the tension when the temperature of the wire falls to  $0^{\circ}\text{C}$ . Assume that the distance between the supports remains constant. ( $Y = 2.1 \times 10^{11}\text{ N/m}^2$ ,  $\alpha = 12 \times 10^{-6}/^{\circ}\text{C}$ )
3. Ice of mass of 2 kg at  $-20^{\circ}\text{C}$  and 5 kg water at  $20^{\circ}\text{C}$  are mixed (specific heat of water =  $1\text{ Cal/g}^{\circ}\text{C}$ , specific heat of ice =  $0.5\text{ cal/g}^{\circ}\text{C}$ ) Find the net amount of water in the container.
4. A vessel contains a mixture of 7 gm of nitrogen and 11 gm of carbon dioxide at room temperature  $T = 290\text{ K}$ . If the pressure of the mixture  $P = 1\text{ atm}$ , calculate its density. ( $R = 8.31\text{ J/mol K}$ )
5. Find the average translation kinetic energy per molecule if one mole of the gas is contained in a volume  $1.23 \times 10^{-3}\text{ m}^3$  at a pressure  $2 \times 10^5\text{ N/m}^2$ . Avogadro's number is  $6.02 \times 10^{23}$  molecules/mole.
6. The molar heat capacity of a process varies as  $C = C_V + \alpha V$ , where  $\alpha$  is constant. Find the equation of the process in the V-T variable.
7. A horizontal cylindrical tube of cross-sectional area A fitted with two frictionless pistons. The pistons are connected to each other by an inextensible wire. Initially, the temperature of the gas is  $T_0$  and its pressure is  $p_0$  which equals the atmospheric pressure. Find the tension in the wire if the wire temperature is raised to  $3T_0$ .
8. A gas has been subjected to an isochoric- isobaric cycle 1-2-3-4-1. Plot the graph of this cycle in the P-p, V-T and P-T coordinates.  
( $\rho =$  density of the gas)



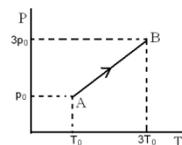
9. An ideal monoatomic gas undergoes a cyclic process as shown in the P-V diagram. For each process find
  - (a) the work done
  - (b) the change in internal energy and
  - (c) the heat transfer. Also find the efficiency of the cycle.



10. The ideal gas of mass m follows a process from state  $(P_0, 2V_0)$  to  $(2P_0, V_0)$ . What maximum/ minimum temperature will the gas reach in this process, if it is depicted on the P-V diagram as a straight line as shown in the figure. The molecular weight of the gas is M



11. The volume of a moles of an ideal gas with the adiabatic exponent  $\gamma$  is varied according to the law  $V = a/T$ , where a is a constant. Find the amount of heat received by the gas in this process if the gas temperature is increased by  $\Delta T$ .
12. A monoatomic gas undergoes a cycle consisting of two isothermal and two isobars. If the minimum and maximum temperature of the gas during the cycle are  $T_1 = 400\text{ K}$  and  $T_2 = 800\text{ K}$ , respectively, and the ratio of maximum to minimum volume is 4, calculate the efficiency of the cycle.
13. Two moles of a monoatomic ideal gas undergoes a process AB as shown in the figure. Find:
  - (a) the work done; and
  - (b) the heat transfer during the process.



## PART- B OBJECTIVE

### ( MULTI CHOICE SINGLE CORRECT)

1. The radius of a ring is  $R$  and its coefficient of linear expansion is  $\alpha$ . If the temperature of the ring increases by  $\theta$ , then its circumference will increase by

- a)  $\pi R\alpha\theta$  b)  $2\pi R\alpha\theta$  c)  $\pi R\alpha\theta/2$  d)  $\pi R\alpha\theta/4$

2. There are two spheres of same material and radius. One is solid and the other is hollow. If they are heated to the same temperature, the expansion of:

- a) solid sphere is more b) hollow sphere is more  
c) solid and hollow spheres are equal  
d) solid is outward while that of hollow inwards

3. When a strip made of iron  $\alpha_1$  and copper  $\alpha_2 (>\alpha_1)$  is heated:

- a) its length does not change b) it gets twisted  
c) it bends with iron on concave side  
d) it bends with iron on convex side

4. Equal masses of three liquids A, B and C have temperatures  $10^\circ\text{C}$ ,  $25^\circ\text{C}$  and  $40^\circ\text{C}$ , respectively. If A and B are mixed, the mixture has a temperature of  $15^\circ\text{C}$ . If B and C are mixed, the mixture has a temperature of  $30^\circ\text{C}$ . If A and C are mixed, the mixture has a temperature of

- a)  $16^\circ\text{C}$  b)  $20^\circ\text{C}$  c)  $29^\circ\text{C}$  d)  $25^\circ\text{C}$

5. During an experiment, an ideal gas is found to obey the equation  $P^2V = \text{constant}$ . The gas is initially at temperature  $T$  and volume  $V$ . When it expands to a volume  $2V$ , the temperature becomes

- a)  $\sqrt{2}T$  b)  $T/2$  c)  $\sqrt{3}T$  d)  $2T$

6. The bulk modulus of elasticity for a monoatomic ideal gas during an isothermal process is ( $P =$  pressure of the gas)

- a)  $P$  b)  $2P/3$  c)  $5P/3$  d)  $7P/5$

7. The mass of hydrogen molecule is  $3.32 \times 10^{-27}$  kg. If  $10^{23}$  hydrogen molecules strike per seconds at  $2 \text{ cm}^2$  area of rigid wall at an angle of  $45^\circ$  from the normal and rebound back with a speed of  $1000 \text{ m/s}$ , then the pressure exerted on the wall is

- a)  $2.34 \times 10^3$  pascal b)  $0.23 \times 10^3$  pascal  
c)  $0.23 \times 10^3$  pascal d)  $23.4 \times 10^3$  pascal

8. The number of molecules per unit volume of a gas is given by

- a)  $P/kT$  b)  $kT/P$  c)  $P/RT$  d)  $RT/P$

where  $R$  and  $k$  are universal gas constant and Boltzmann's constant, respectively.

9. A gas is filled in a container at pressure  $P_0$ . If the mass of molecules is halved and their rms speed is doubled, then the resultant pressure will be

- a)  $P_0$  b)  $4P_0$  c)  $2P_0$  d)  $P_0/2$

10. When an ideal diatomic gas is heated at constant pressure, then the fraction of heat energy which is used to increase the internal energy of gas system, is

- a)  $3/7$  b)  $3/5$  c)  $5/7$  d)  $2/5$

11. The velocities of three molecules are  $3v$ ,  $4v$  and  $5v$ . Their rms speed will

- a)  $\sqrt{50}/\sqrt{3}v$  b)  $\sqrt{3}/\sqrt{50}v$  c)  $50/3v$  d)  $3/50v$

12. A gas mixture consists of 2 moles of  $\text{O}_2$  and 4 moles of Ar at a temperature  $T$ . Neglecting all vibrational moles, the total internal energy of the system is

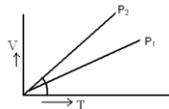
- a)  $4RT$  b)  $15RT$  c)  $9RT$  d)  $11RT$

13. For a certain gas, the ratio of specific heats is  $3/2$ . What is the value of  $C_p$ ?

- a)  $R$  b)  $2R$  c)  $3R$  d)  $5R$

14. In the following V-T diagram, what is the relation between  $P_1$  and  $P_2$ ?

- a)  $P_2 = P_1$  b)  $P_2 > P_1$  c)  $P_2 < P_1$  d) cannot be predicted



15. The average degree of freedom per molecule for a gas is 6. The gas performs 25J of work when it expands at constant pressure. The heat absorbed by the gas is

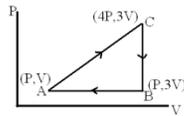
- a) 75J b) 100J c) 150J d) 125J

16. When the state of a system is changed from A to B adiabatically, work done on the system is 322 joule. Then, the state of the system is changed from A to B by another method which requires 100J of heat. The work done on the system in this process will be

- a) 222 joule b) 100 joule c) 422 joule d) 322 joule

17. An ideal gas is taken through a series of changes represented in figure. The total work done by the gas at the end of the cycle is equal to

- a) zero      b) 2PV      c) 3PV      d) 5PV



18. If one mole of a monoatomic gas is mixed with one mole of a diatomic gas, the value of  $\gamma$  for the mixture is  
 a) 1.40      b) 1.50      c) 1.53      d) 3.07
19. A bucket full of hot water is kept in a room and it cools from  $75^\circ\text{C}$  to  $70^\circ\text{C}$  in  $T_1$  minutes, from  $70^\circ\text{C}$  to  $65^\circ\text{C}$  in  $T_2$  minutes and from  $65^\circ\text{C}$  to  $60^\circ\text{C}$  in  $T_3$  minutes. Then,  
 a)  $T_1 = T_2 = T_3$       b)  $T_1 < T_2 < T_3$       c)  $T_1 > T_2 > T_3$       d)  $T_1 < T_2 > T_3$
20. The formation of ice is started in a lake with water at  $0^\circ\text{C}$  when the atmospheric temperature is  $-10^\circ\text{C}$ . If time taken for 1 cm of ice to be formed is 7 hours, the time taken for the thickness of ice to increase from 1 cm to 2 cm is  
 a) less than 7 hours      b) 7 hours      c) more than 14 hours  
 d) more than 7 hours but less than 14 hours
21. Two stars  $S_1$  and  $S_2$  radiate maximum energy at 360 nm and 480 nm, respectively. Ratio of their absolute temperature is  
 a) 3/4      b) 4/3      c) 9/16      d) 16/9

### MULTI CHOICE MULTI CORRECT

- A solid sphere and a hollow sphere of the same material and of equal radii are heated to the same temperature.
  - Both will emit equal amount of radiation per unit time in the beginning.
  - Both will absorb equal amount of radiation from the surrounding in the beginning.
  - The initial rate of cooling ( $dT/dt$ ) will be the same for the two spheres.
  - The two spheres will have equal temperatures at any instant.
- One gram of water becomes  $1671\text{ cm}^3$  of steam when boiled at atmospheric pressure.  $L_v = 540\text{ cal/gm}$  [  $1\text{ atm} = 1.01 \times 10^5\text{ N/m}^2$  ]
  - Then internal energy change is 499.7 cal
  - The work done 40.3 cal
  - Heat exchange is 540 cal
  - Volume change is not possible
- The molar heat capacity for an ideal gas
  - is zero for an adiabatic process
  - is infinite for an isothermal process
  - depends only on the nature of the gas for a process in which either volume or pressure is constant
  - is equal to the product of the molecular weight and specific heat capacity for any process.

### NUMERICAL BASED TYPE

- A composite bar of length  $L = L_A + L_B$  is made from a bar of metal A (coefficient of linear expansion is  $1.4 \times 10^{-5}/^\circ\text{C}$ ) and length  $L_A = L_0$ , attached to a bar of metal B (coefficient of linear expansion is  $0.2 \times 10^{-5}/^\circ\text{C}$ ) and  $K \times 10^{-6}/^\circ\text{C}$ , then find the value of K.
- In an insulated vessel, 0.05 kg steam at 373 K and 0.45 kg of ice at 253 K are mixed. Then find the final temperature of the mixture in  $^\circ\text{C}$ . Given  $L_{\text{fusion}} = 80\text{ cal/g} = 336\text{ J/g}$ ,  $L_{\text{vaporization}} = 540\text{ cal/g} = 2268\text{ J/g}$ ,  $S_{\text{ice}} = 2100\text{ J/kg}$   $K = 0.5\text{ cal/gK}$  and  $S_{\text{water}} = 4200\text{ J/kg}$   $K = 1\text{ cal/gK}$
- One mole of a gas ( $\gamma = 5/3$ ) is initially at temperature  $27 = 5/3$  is initially at temperature  $27^\circ\text{C}$  and occupy a volume  $V$ . The gas is first expanded at constant pressure until its volume double. Then it undergoes an adiabatic change until the temperature returns to its initial value. If the total work done in the process  $\lambda$  ( $150R$ ) Joule, then find the value of  $\lambda$ . ( $R$  is the gas constant)
- A metal ball of mass  $m$  is heated by means of a 18 watt heater in a room at  $20^\circ\text{C}$ . The temperature of ball becomes steady at  $50^\circ\text{C}$ . Assuming Newton's law of cooling, calculate the rate of loss of heat in watt to the surrounding when the ball is at  $30^\circ\text{C}$ .